Vectors

An **array** is a collection of numbers, called **elements**, referenced by one or more indices running over different index sets. In MATLAB, the index sets are always sequential integers starting with 1. The **dimension** of the array is the number of indices needed to specify an element. The **size** of an array is a list of the sizes of the index sets.

A **matrix** is a two-dimensional array with special rules for addition, multiplication, and other operations. The two dimensions are called the **rows** and the **columns**.

A vector is a matrix in which one dimension has only the index 1. A row vector has only one row and a **column vector** has only one column.

1. Entering Vectors and Matrices

There are several ways to enter vectors and matrices in Matlab. These include:

1- Entering an explicit list of elements.

2- Loading matrices from external data files.

3- Generating matrices using functions.

To enter a vector or matrix explicitly, there are a few basic rules to follow:

• Separate the elements of a row with spaces or commas.

• Use a semicolon ; or returns, to indicate the end of each row.

• Surround the entire list of elements with square brackets, [].

For example, to input a 3×1 vector:

>> u=[1 2 3]

```
u =
```

1 2 3

The entries must be enclosed in square brackets.

```
>> v =[ 1 3 sqrt(5)]
```

v =

```
1.0000 3.0000 2.2361
```

Spaces is very important:

```
>> v2 =[3+4 5]
v2 =
7 5
>> v3 =[3 +4 5]
v3 =
3 4 5
```

We can do certain arithmetic operations with vectors of the same length, such as v and v3 in the previous section.

```
>> v + v3
ans =
  4.0000 7.0000 7.2361
>> v4 =3*v
v4 =
  3.0000 9.0000 6.7082
>> v5 =2*v -3*v3
v5 =
  -7.0000 -6.0000 -10.5279
We can build row vectors from existing ones:
>> w =[1 2 3], z = [8 9]
w =
   1
       2
           3
z =
   8
       9
>> v6=[w z]
v6 =
   1
       2
            3
                8
                     9
A vector can be defined by previously defined vectors.
>> x = [2 4 -1]
X =
       4 -1
   2
>> x1 = [x 58]
x1 =
```

2 4 -1 5 8

An special array is the **empty matrix**, which is entered as [] .and can be used to delete a part of any matrix or vector.

```
>> w=[4 5 6 7]
w =
4 5 6 7
>>w(4)=[];w
w =
4 5 6
```

The elements of a matrix can be defined with algebraic expressions placed at the appropriate location of the element. Thus

>> a = [sin(pi/2) sqrt(2) 3+4 6/3 exp(2)]

a =

1.0000 1.4142 7.0000 2.0000 7.3891

2. Column Vectors

The column vectors have similar constructs to row vectors. When defining them, entries are separated by ; or "newlines".

Note how the column vector is defined, using brackets and semicolons to separate the different rows. To define a column vector x:

```
x=[1; -2; 4]
X =
1
-2
4
or write
>>x=[1
2
3]
X =
1
-2
4
>> c =[ 1; 3; sqrt(5)]
c =
1.0000
3.0000
2.2361
```

3. Transposing

We can convert a row vector into a column vector (and vice versa) by a process called *transposing*, denoted by '

```
> A=[ 1 2 3]
A =
1 2 3
>>B= A'
B =
1
2
```

3

4. Vectors Addition and subtraction

Addition and subtraction of a number to or from a vector can be made. In this case, the number is added to or subtracted from all the elements of the vector. For example

```
>> x=[-1; 0; 2];
>> y=x-1
y =
-2
-1
1
```

If we look to make a simple addition and subtraction of vectors. The notation is the same as found in most linear algebra. We will define two vectors then add or subtract them:

```
>> v = [1; 2; 3]
v =
   1
   2
   3
>> b = [2; 4; 6]
b =
   2
   4
   6
>> v+b
ans =
   3
   6
   9
>> v-b
ans =
  -1
  -2
  -3
>> sin(v)
ans =
```

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```
0.8415
0.9093
0.1411
>> log(v)
ans =
0
0.6931
1.0986
>> pi*v
ans =
3.1416
6.2832
9.4248
```

5. Vectors multiplication

Multiplication of vectors and matrices must follow special rules. In the example above, the vectors are both column vectors with three entries. You cannot add a row vector to a column vector. In the case of multiplication vectors, the number of columns of the vector on the left must be equal to the number of rows of the vector on the right.

```
>> b = [2; 4; 6];
>> v = [1; 2; 3];
>> v*b
??? Error using ==> *
Inner matrix dimensions must agree.
>> v*b'
ans =
   2
       4
           6
   4
           12
       8
      12
           18
   6
>> v'*b
ans =
  28
```

6. element-wise operation

There are many times where we want to do an operation to every entry in a vector or matrix. Matlab will allow you to do this with "element-wise" operations. For example, suppose you want to multiply each entry in vector v with its corresponding entry in vector

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b. In other words, suppose you want to find v(1)*b(1), v(2)*b(2), and v(3)*b(3). It would be nice to use the "*" symbol since you are doing some sort of multiplication, but since it already has a definition, we have to come up with something else. The programmers who came up with Matlab decided to use the symbols ".*" to do this.

>> v.*b
ans =
 2
 8
 18
Also for division we must use "./"
>> v./b
ans =
 0.5000
 0.5000
 0.5000

Note that

v .* b multiplies each element of v by the respective element of b.

v ./ b divides each element of v by the respective element of b.

 $v \land b$ divides each element of b by the respective element of v.

v.[^] b raise each element of v by the respective b element.

7. The Colon Operator

The colon operator ': ' is understood by 'matlab' to perform special and useful operations. If two integer numbers are separated by a colon, 'matlab' will generate all of the integers between these two integers.

In particular, you will be able to use it to extract or manipulate elements of matrices. The following command creates a row vector whose components increase arithmetically:

>> 1:5

ans =

12345

And, if three numbers, integer or non-integer, are separated by two colons, the middle number is interpreted to be a "step" and the first and third are interpreted to be "limits". Thus

```
>> b = 0.0 : 0.2 : 1.0
b =
0 0.2000 0.4000 0.6000 0.8000 1.0000
```

Suppose you want to create a vector with elements between 0 and 20 evenly spaced in increments of 2. Then you have to type:

>> t = 0:2:20 t = 8 10 12 14 16 2 4 6 18 0 20 >> m=0.32:0.1:0.6 **m** = 0.3200 0.4200 0.5200 >>w= -1.4:-0.3:-2 w = -1.4000 -1.7000 -2.0000

The format is **first:step:last**. The result is always a row vector.

A negative step is also allowed. The command has similar results; it creates a vector with linearly spaced entries.

There is another way to create row arrays is to use linspace functions:

```
>> A=linspace(1,2,5)
A =
  1.0000
         1.2500 1.5000
                           1.7500
                                   2.0000
>> A=linspace(0,20,11)
A =
   0
      2
          4
              6
                  8
                     10
                          12
                             14 16
                                       18
                                            20
```

8. Referencing elements

It is frequently necessary to call one or more of the elements of a vector. Each dimension is given a single index. Some examples using the definitions above:

Evaluate a vector A:

```
>> A=0:10:100
A =
      10
                     40
                          50
                               60
   0
           20
                30
                                   70
                                        80
                                             90 100
Now after definition of a vector A, try to type:
>> A(10)
ans =
  90
>> B=A(1:5)
B =
   0
      10 20
                30
                     40
>> C=A(1:2:10)
C =
```

0 20 40 60 80 >> A(6:2:10) ans = 50 70 90

9. Other Operations on Vectors

MATLAB has a large number of built-in functions. You will only become familiar with them by using them. Try to make the vector \mathbf{v} in command window and use the functions below. v=[23 0 3 16 -8 13] length(v) number of elements in v. 6 **size(v)** size of matrix v (raw, column). 1 6 **find(v)** finds indices of non-zero elements. 4 3 5 1 6 find(v==0) finds indices of elements equal to zero. 2 find(v==16) finds indices of elements equal to 16. 4 find(v>7) finds indices of elements greater than 7. 1 4 6 **v(find(v>7))** finds the values of elements greater than 7. 16 13 23 **sum(v)** sum of elements 47 **max(v)** maximum element. 23 **min(v)** minimum element. -8 **mean(v)** mean of elements. 7.8333 **sort(v)** sorts elements from minimum to maximum value.

-8 0 3 13 16 23

all(v) equal to 1 if all elements nonzero, 0 if any element nonzero.
0
abs(v) vector with absolute value of all element
23 0 3 16 8 13

Exercise 1:

Calculate Reynold Number at a diameter D=0.2 m, using different velocity's as $u=0.1,0.2,0.3 \dots 1$ m/s knowing that:

```
Re=(\rho ud)/\mu, \mu=0.001, \rho=1000
    Solution:
    Type the code in the command window
    d=0.2;
    u=0.1:0.1:1;
    m=0.001;
    p=1000;
    Re=u*p*d/m
    The results will be
    Re =
    1.0e+005 *
    0.2000
             0.4000
                       0.6000
                                0.8000
                                          1.0000
                                                    1.2000
                                                             1.4000
                                                                       1.6000
1.8000 2.0000
```

Exercise 2:

Estimate the average density of a Water/Ethanol mixture at different water compositions knowing that.

Water density =1000 kg/m³ Ethanol density =780 kg/m³ Mixture density = Xwater × Water density + Xethanol × Ethanol density

```
Solution:

Pwater=1000;

Pethanol=780;

Xwater=0:.1:1;

Xethanol=1-Xwater;

Pav=Pwater*Xwater+Pethanol*Xethanol
```

```
Xwater =
```

0 0.1000 0.2000 0.3000 0.4000 0.5000 0.6000 0.7000 0.8000 0.9000 1.0000

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Pa	av =							
	780	802	824	846	868	890	912	934
956	978	1000						

Exercise 3:

Write a program to calculate average density, conductivity and specific heat for water in the range of temperatures from 0 to 50 C. Knowing that this parameters for water are a function of temperature such as the following equations.

The Density

 $\rho = 1200.92 - 1.0056 \; T_{K}{}^{o} + 0.001084 \; * \; (T_{K}{}^{o})^{2}$

The condactivity

 $K = 0.34 + 9.278 * 10^{-4} .T_{K}^{\circ}$

The Specific heat

 $C_P = 0.015539 (T_K^{\circ} - 308.2)^2 + 4180.9$ Note: take 11 point of temperatures

```
Solution:

T=[0:5:50]+273;

p=1200.92 - 1.0056*T+ 0.001084 * T.^2;

Kc = 0.34 + 9.278 * 10^{-4} *T;

Cp = 0.015539*(T - 308.2).^{2} + 4180.9;

Average_density=mean(p)

Average_conductivity=mean(Kc)

Average_specificheat=mean(Cp)

Gives the results

Averagedensity =

997.7857

Averageconductivity =

0.6165

Averagespecificheat =

4.1864e+003
```

Practice Problems

1. Let x = [2 5 1 6].

- a) Add 16 to each element.
- b) Add 3 to just the odd-index elements.
- c) Compute the square root of each element.
- d) Compute the square of each element.
- 2. Let $x = [3 \ 2 \ 6 \ 8]$ and $y = [4 \ 1 \ 3 \ 5]$
 - a) Add the elements in x to y
 - b) Raise each element of x to the power specified by the corresponding element in y.
 - c) Divide each element of y by the corresponding element in x
 - d) Multiply each element in x by the corresponding element in y, calling the result "z".
- 3. When A and B contain the values shown below, give the values of C vector after executing the following statements.

$$A = [2 - 15 0] ; B = [3 2 - 1 4]$$

- a) C = A-B
- b) C = B + A 3
- c) C = B./A
- d) $C = A.^B$
- e) $C = 2.^B+A$
- f) $C = 2*A+A.^B$
- 4. Use the **linspace** commands to create 4 vectors a, b, c, d with the elements:
 - a) 2, 4, 6, 8... to 10 elements
 b) 10, 8, 6, 4, 2, 0, -2, -4...to 15 elements
 c) 1, 1/2, 1/3, 1/4, 1/5... to 10 elements
 d) 0, 1/2, 2/3, 3/4, 4/5... to 10 elements
- 5. Compute the average molecular weight of a mixture of <u>equal</u> fractions of CH₄, H₂, O₂, CO, CO₂, H₂O, CH₃OH, C₂H₆.

The average molecular weight: $Mw_{average} = \sum_{i=1}^{N_c} Mw_i \times x_i$